

# C.U.SHAH UNIVERSITY

## Summer Examination-2018

Subject Name : Advanced Mathematics

Subject Code : 2TE02AMT1

Branch: Diploma (All)

Semester : 2

Date : 25/04/2018

Time : 10:30 To 01:30

Marks : 70

Instructions:

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

Q-1

Attempt the following questions:

(14)

- a) If  $P(-5, 7)$  and  $Q(7, -2)$  then  $PQ = \underline{\hspace{2cm}}$ .  
(A) 15 (B) 169 (C)  $\sqrt{29}$  (D) None of these
- b) If  $A(2, -7)$  and  $B(4, 3)$  are the given points, find the midpoint of AB.  
(A)  $(-2, 5)$  (B)  $(3, -2)$  (C)  $(2, 5)$  (D)  $(5, 2)$
- c) x – intercept of line  $3x + 2y - 7 = 0$  is  $\underline{\hspace{2cm}}$ .  
(A)  $7/2$  (B)  $-7/2$  (C)  $7/3$  (D)  $-7/3$
- d) Centre of the circle  $2x^2 + 2y^2 = 5$  is  $\underline{\hspace{2cm}}$ .  
(A)  $(0, 0)$  (B)  $(5, 0)$  (C)  $(0, 5)$  (D)  $(5/2, 5/2)$
- e)  $\lim_{x \rightarrow 0} \frac{5^x - 1}{x} = \underline{\hspace{2cm}}$   
(A) 0 (B)  $e^5$  (C)  $\log_e 5$  (D) 1
- f)  $\lim_{x \rightarrow 2} \frac{x^3 - 8}{x - 2} = \underline{\hspace{2cm}}$   
(A) 4 (B) 0 (C) 1 (D) 12
- g)  $\lim_{x \rightarrow 0} \frac{\sin 4x}{\tan 7x} = \underline{\hspace{2cm}}$   
(A)  $7/4$  (B)  $4/7$  (C) 1 (D) None of these
- h)  $\frac{d(\sqrt{x})}{dx} = \underline{\hspace{2cm}}$   
(A)  $\frac{1}{2\sqrt{x}}$  (B)  $\frac{1}{\sqrt{x}}$  (C)  $-\frac{1}{x^2}$  (D)  $2\sqrt{x}$
- i)  $\frac{d(\tan x)}{dx} = \underline{\hspace{2cm}}$   
(A)  $\cos ec^2 x$  (B)  $-\cos ec^2 x$  (C)  $-\sec^2 x$  (D)  $\sec^2 x$



- j)  $\frac{d(x^x)}{dx} = \underline{\hspace{2cm}}$   
 (A)  $x^x \log x$  (B)  $x^x(1 + \log x)$  (C)  $x \log x$  (D)  $x(1 + \log x)$
- k)  $\frac{d(\sin^{-1} x + \cos^{-1} x)}{dx} = \underline{\hspace{2cm}}$   
 (A)  $\frac{\pi}{2}$  (B)  $-1$  (C)  $0$  (D)  $1$
- l)  $\int \sec x \, dx = \underline{\hspace{2cm}}$   
 (A)  $\log|\sec x + \tan x| + c$  (B)  $\log|\cos ecx - \cot x| + c$  (C)  $\log|\sec x| + c$   
 (D)  $\log|\sin x| + c$
- m)  $\int \frac{1}{a^2 + x^2} \, dx = \underline{\hspace{2cm}}$   
 (A)  $\frac{1}{a} \cot^{-1} \frac{x}{a} + c$  (B)  $\cos^{-1} \frac{x}{a} + c$  (C)  $\frac{1}{a} \tan^{-1} \frac{x}{a} + c$  (D)  $\sin^{-1} \frac{x}{a} + c$
- n)  $\int_2^5 x^3 \, dx = \underline{\hspace{2cm}}$   
 (A)  $\frac{641}{4}$  (B)  $\frac{609}{4}$  (C)  $\frac{690}{4}$  (D)  $\frac{614}{4}$

**Attempt any four questions from Q-2 to Q-8**

**Q-2 Attempt all questions (14)**

- a) In which ratio Y – axis divides line segment joining points (1, 2) and (2, 1)? Find co ordinates of division point. (5)
- b) Find the equation of straight line passing through (4, 3) and perpendicular to line  $4y - 3x + 7 = 0$ . (5)
- c) If  $f(x) = \frac{ax+b}{bx+a}$  then prove that  $f(x) \cdot f\left(\frac{1}{x}\right) = 1$ . (4)

**Q-3 Attempt all questions (14)**

- a) Prove that  $\lim_{x \rightarrow 0} \frac{2(5^x) + 3(2^x) - 5}{x} = \log_e 200$ . (5)
- b) Evaluate:  $\lim_{x \rightarrow \frac{\pi}{4}} \frac{2 - \sec^2 x}{1 - \tan x}$  (5)
- c) Prove that the points (0, -3), (1, -2) and (10, 7) are collinear. (4)

**Q-4 Attempt all questions (14)**

- a) Find equation of a circle passing through points (2, 0), (0, 2) and (0, 0). (5)
- b) Find derivative of  $f(x) = x^3 - 2x$  using definition. (5)
- c) Find  $\frac{dy}{dx}$  if  $y = \frac{x^2 - 1}{x^2 + 1}$ . (4)

**Q-5 Attempt all questions (14)**

- a) Evaluate:  $\lim_{x \rightarrow a} \frac{\sqrt{2a-x} - \sqrt{x}}{a-x}$  (5)



b) The equation of motion of a particle is  $S = t^3 - 3t^2 + 4t + 3$ . Find velocity and acceleration at  $t = 2$ . (5)

c) Find  $\frac{dy}{dx}$  if  $y = (\sin x)^x$ . (4)

**Q-6**

**Attempt all questions**

(14)

a) Evaluate:  $\int \left[ \sqrt{1 + \sin 2x} + \sqrt{\frac{1 + \cos 2x}{1 - \cos 2x}} \right] dx$  (5)

b) Find  $\frac{dy}{dx}$  if  $e^x + e^y = e^{x+y}$ . (5)

c) Evaluate:  $\int x \log x \, dx$  (4)

**Q-7**

**Attempt all questions**

(14)

a) Find  $\frac{dy}{dx}$  if  $y = \log \left( \frac{\sin x}{1 + \cos x} \right)$ . (5)

b) Evaluate:  $\int \left( \sqrt{x} + \frac{1}{\sqrt{x}} \right)^2 dx$  (5)

c) Evaluate:  $\int_0^{10} W \, dx$  Where  $W = \frac{3}{4}x \left( 1 + \frac{x}{10} \right)$  (4)

**Q-8**

**Attempt all questions**

(14)

a) Prove that  $\int_0^{\frac{\pi}{2}} \frac{\tan x}{\tan x + \cot x} \, dx = \frac{\pi}{4}$ . (5)

b) Find the volume of sphere of radius  $r$ . (5)

c) Find centre and radius of circle  $x^2 + y^2 - 4x - 6y - 4 = 0$ . (4)

